

# The Effects of Free Trade Agreements on Product-level Trade

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Celebrating Gravity at 60 - Austrian Institute of Economic Research

December 9, 2022

## Motivation

### **What we think we know about trade agreements and trade costs**

- ▶ Trade liberalization increases trade for all products, to varying degrees
- ▶ Changes in technological comparative advantage are independent of changes in trade costs
- ▶ Gravity estimates of FTA effects using aggregate trade data reflect changes in aggregate trade costs

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- ▶ It's possible that, for a sizeable share of products, trade actually **decreases**

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## What I'm going to try to convince you of

- ▶ Virtually all trade creation following FTAs comes from products that were relatively less traded ex ante
- ▶ It's possible that, for a sizeable share of products, trade actually **decreases**
- ▶ A significant portion of our aggregate FTA estimate reflects changes in bilateral comparative advantages, *not* changes in trade costs.

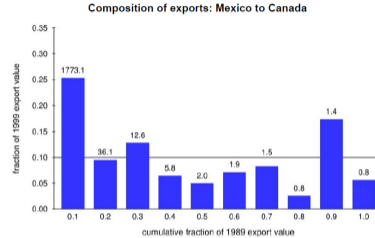
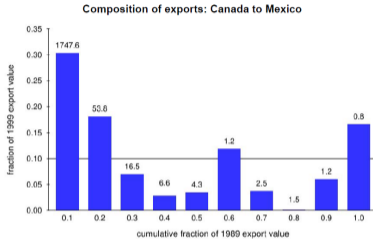
## Motivation

Two provocative findings that serve as our inspiration

1. Baier and Bergstrand (2007): average trade creation effects of FTAs too large to be explained by tariffs
2. Kehoe and Ruhl (2013) critique of CGE model predictions:
  - ◇ Models tended to underpredict trade creation for products that are only lightly-traded *ex ante*
  - ⇒ **Hypothesis**: prevalence of non-traded/lightly trade products creates potential for “explosive trade creation” *ex post*

Surprisingly little work has been done to synthesize these observations

## NAFTA Example from Kehoe and Ruhl (2013)



- ▶ Figures show concentration of Mexico-Canada post-NAFTA trade growth in “least-traded” products (LTPs)
- ▶ Taken from Kehoe and Ruhl (2013)

## Our Objectives (3)

### 1. **Construct new estimates of the *aggregate* effects of FTAs on trade using *product-level* data**

- ◇ Exploit “adding up” properties of PPML to reconcile product-level and aggregate-level estimates.
- ◇ Addresses micro-level “composition bias” in standard estimates using aggregate data
- ◇ Allows us to assess which subsets of products have grown faster than others

### 2. **Test “less-traded products” = “explosive trade growth” story**

- ◇ Data: product-level (5 digit SITC rev 3) trade between 116 countries observed between 1991 and 2015

### 3. **Establish new facts about product-level changes in trade:**

- ◇ Demonstrate aggregation bias in standard estimates based on aggregate data
- ◇ Can isolate how much of trade growth is due to least-traded products vs. moderately and heavily traded products



## What's New?

The related literature generally takes one of two approaches

### “Event study” approach:

- ◇ tend to focus on two-country settings and/or specific agreements  
e.g., Kehoe and Ruhl (2013), Kehoe et al. (2015), Ruhl and Willis (2017), Kohn et al. (2016)
- ◇ **Comment:** cannot disentangle (bilateral) effects of FTA from (multilateral) effects of technological change, comparative advantage, local market conditions, multilateral resistance, exchange rate changes, etc.

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### “Margin decomposition”:

- ◇ decompose aggregate trade growth into extensive / intensive margins  
e.g., Hummels and Klenow (2005), Arkolakis et al. (2008), Baier et al. (2014)
- ◇ **Comment:** once a least-traded product is no longer “least-traded”, it no longer contributes to extensive margin growth, no matter how fast trade grows for that product.

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- ◇ **Comment:** once a least-traded product is no longer “least-traded”, it no longer contributes to extensive margin growth, no matter how fast trade grows for that product.

### Our approach: *Pooled, product-level gravity estimation.*

- ◇ Allows us to extract overall “average partial effects” of FTAs which:
  - i. account for product-level multilateral effects;
  - ii. allow decompositions of trade growth at the product level;
  - iii. address “aggregation bias” in aggregate estimates

## Results

**Main result:** We confirm less-intensively traded products (LTPs) experience relatively faster rates of trade creation after liberalization.

### Details:

- ▶ LTPs contribute ~100% of trade growth following liberalization.
- ▶ The LTP decile (bottom 10%) is the only decile with statistically significant avg. trade growth, across many different specifications.
- ▶ For higher deciles (above 40%), trade growth is always **negative** (!) and significant.
- ▶ **Mean reversion!** Irrespective of FTAs, product-level trade costs generally fall faster for less-traded products vs. more traded products
- ▶ Product-level FTA estimates suggest upward bias in aggregate estimates of trade cost reduction effects of FTAs
  - ◊ Suggests additional channel for FTA trade creation effects: **strengthening in bilateral comparative advantages** that otherwise would be measured as trade cost reductions.

## Related literature

### Estimating the effects of FTAs using panel data:

Baier and Bergstrand (2007); Yotov et al. (2016); Larch et al. (2019); Weidner and Zylkin (2021)

### Product-level gravity and aggregation bias in aggregate-level estimates:

French (2016, 2017)

### The “extensive margin” of trade:

Hummels and Klenow (2005); Arkolakis et al. (2008); Besedeš and Prusa (2011)

### Trade growth in new products following FTAs:

Arkolakis (2010); Kehoe and Ruhl (2013); Baier et al. (2014); Kehoe et al. (2015); Besedeš et al. (2015); Kohn et al. (2016); Ruhl and Willis (2017)

## Aggregate-level Gravity

For *aggregate-level* trade data, the standard gravity equation for estimating FTA effects is well-known:

$$X_{ijt} = \exp(\delta_{it} + \psi_{jt} + \eta_{ij} + \beta \mathbf{FTA}_{ijt}) + \varepsilon_{ijt}. \quad (1)$$

- ◇  $\mathbf{FTA}_{ijt}$ : a set of (time-varying) dummies for the presence of a bilateral trade agreement.
- ◇  $\delta_{it}$  and  $\psi_{jt}$ : *exporter-time* and *importer-time* FEs to account for GE terms
- ◇  $\eta_{ij}$ : *time-invariant* bilateral FE to absorb ex ante trade frictions
- ◇ PPML leads to consistent estimates (Santos Silva and Tenreyro, 2006; Weidner and Zylkin, 2021)

**Baseline objective:** estimate  $\beta$ , the “average partial effect” of signing a trade agreement.

## Pooled, Product-level Gravity

To account for **aggregation bias**, our proposed alternative is *pooled, product-level* gravity

$$X_{ijkt} = \exp(\delta_{ikt} + \psi_{jkt} + \eta_{ijk} + \beta \mathbf{FTA}_{ijt}) + \varepsilon_{ijkt}. \quad (2)$$

- ◇  $\delta_{ikt}, \psi_{jkt}$ : *exp-product-time* and *imp-product-time* FEs to account for changes in comp. advantage, demand patterns
- ◇  $\eta_{ijk}$ : time-invariant *product-pair* FE to account for product-level heterogeneity in ex ante trade barriers

### Baseline objective remains the same:

Estimate the “average partial effect” of signing a trade agreement on *aggregate* trade flows, only now pooling across product-level trade flows.

## Pooled, Product-level Gravity

To account for **aggregation bias**, our proposed alternative is *pooled, product-level* gravity

$$X_{ijkt} = \exp(\delta_{ikt} + \psi_{jkt} + \eta_{ijk} + \beta \mathbf{FTA}_{ijt}) + \varepsilon_{ijkt}. \quad (2)$$

To test if least-traded products grow faster than other products, we use

$$X_{ijkt} = \exp\left(\delta_{ikt} + \psi_{jkt} + \eta_{ijk} + \beta_1 \mathbf{FTA}_{ijt} + \beta_2 \mathbf{FTA}_{ijt} \times \mathbf{1}_{k \notin \Omega_{ij}^*}\right) + \varepsilon_{ijkt}, \quad (3)$$

where  $\mathbf{1}_{k \notin \Omega_{ij}^*}$  equals 1 if  $k$  was a “least traded product” before  $i$  and  $j$ 's agreement



## PPML and Consistent Aggregation Across Products

**It adds up!** The product-level PPML model nests the aggregate model as special case:

$$\delta_{it} : \sum_j \sum_k X_{ijkt} - \exp [\delta_{it} + \psi_{jt} + \eta_{ij} + \beta \mathbf{FTA}_{ijt}] = 0$$

$$\psi_{jt} : \sum_i \sum_k X_{ijkt} - \exp [\delta_{it} + \psi_{jt} + \eta_{ij} + \beta \mathbf{FTA}_{ijt}] = 0$$

$$\eta_{ij} : \sum_t \sum_k X_{ijkt} - \exp [\delta_{it} + \psi_{jt} + \eta_{ij} + \beta \mathbf{FTA}_{ijt}] = 0$$

$$\beta : \sum_{\mathbf{FTA}=1} \sum_k X_{ijkt} - \exp [\delta_{it} + \psi_{jt} + \eta_{ij} + \beta \mathbf{FTA}_{ijt}] = 0,$$

$\sum_k X_{ijkt} = X_{ijt}$  ensures FOCs consistently aggregate if  $\delta_{ikt} = \delta_{it}$ ;  $\psi_{jkt} = \psi_{jt}$ ;  $\eta_{ijk} = \eta_{ij}$ .

⇒ product-level estimates should be directly comparable with aggregate estimates

⇒ enables us to explicitly assess product-level heterogeneity, differential rates of trade growth.

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⇒ enables us to explicitly assess product-level heterogeneity, differential rates of trade growth.

# Data Sources

## Trade data: UN COMTRADE (5 digit SITC sitc rev3, 1991-2015, manufacturing only)

- ▶ The most disaggregated level for SITC trade (2,771 manufacturing products)
- ▶ Due to switches in code assignments from SITC rev. 2 to HS/SITC rev. 3, we only include countries after they adopt SITC rev. 3. [▶ more](#)
- ▶ 116 largest countries by average annual trade volume, every 4 years
- ▶ Product-level model involves 3 million - 10 million FEs, depending on specification

## Preferential trade agreements

- ▶ FTAs from NSF-Kellogg Database (Baier et al., 2014), which we extend ourselves to 2015
- ▶ Breaks out PTAs/FTAs into multiple categories based on depth of liberalization

[▶ countries](#)

[▶ FTAs](#)

## Aggregate-level Results

| Dependent variable: Aggregate Manufacturing Flows, 1991-2015 |                     |                     |                     |                     |                     |                     |                     |                     |
|--|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|  | PPML                |                     |                     |                     |                     |                     | OLS                 |                     |
|  | (1)                 | (2)                 | (3)                 | (4)                 | (5)                 | (6)                 | (7)                 | (8)                 |
| All FTAs   | 0.113***<br>(0.034) |                     |                     | -0.021<br>(0.046)   | 0.157***<br>(0.033) |                     |                     |                     |
| All FTAs, 4 yr lag   |                     |                     |                     | 0.142***<br>(0.043) |                     |                     |                     |                     |
| All FTAs, lead   |                     |                     |                     |                     | -0.051<br>(0.037)   |                     |                     |                     |
| Regular FTAs   |                     | 0.112***<br>(0.034) | 0.102***<br>(0.039) |                     |                     | -0.030<br>(0.046)   | 0.110***<br>(0.034) | 0.144***<br>(0.031) |
| Regular FTAs, 4 yr lag                                       |                     |                     |                     |                     |                     | 0.150***<br>(0.043) |                     |                     |
| Deep FTAs  |                     | 0.155***<br>(0.054) | 0.141**<br>(0.058)  |                     |                     | 0.125<br>(0.086)    | 0.149***<br>(0.053) | 0.314***<br>(0.053) |
| Deep FTAs, 4 yr lag  |                     |                     |                     |                     |                     | 0.035<br>(0.077)    |                     |                     |
| GSP  |                     |                     | -0.007<br>(0.046)   |                     |                     |                     |                     |                     |
| Non-FTA PTAs   |                     |                     | -0.043<br>(0.048)   |                     |                     |                     |                     |                     |
| <i>Total FTA Effects (main effect + 4 year lag)</i>          |                     |                     |                     |                     |                     |                     |                     |                     |
| All FTAs, total  |                     |                     |                     | 0.121***<br>(0.034) |                     |                     |                     |                     |
| Regular FTAs, total  |                     |                     |                     |                     |                     | 0.120***<br>(0.034) |                     |                     |
| Deep FTAs, total   |                     |                     |                     |                     |                     | 0.161***<br>(0.054) |                     |                     |
| Exporter-time FEs  | x                   | x                   | x                   | x                   | x                   | x                   | x                   | x                   |
| Importer-time FEs  | x                   | x                   | x                   | x                   | x                   | x                   | x                   | x                   |
| Pair FEs   | x                   | x                   | x                   | x                   | x                   | x                   | x                   | x                   |
| "Zeroes"   | x                   | x                   | x                   | x                   | x                   | x                   |                     |                     |
| Observations   | 60614               | 60614               | 60614               | 60614               | 60614               | 60614               | 56201               | 56201               |

Uncorrected PPML estimates for bilateral manufacturing trade flows between 116 countries over the period 1991-2015, using every 4 years. "Deep" FTA refers to customs unions and/or common markets. Standard errors, which appear in parentheses, are clustered by pair. \*  $p < 0.10$ , \*\*  $p < .05$ , \*\*\*  $p < .01$ .

## Extensive Margin / Intensive Margin Decomposition

As in Baier et al. (2014), we can use a Hummels and Klenow (2005) decomposition of aggregate trade flows to measure to what extent FTAs promote trade in more products (*extensive margin*) vs. more trade in products that are already traded (*intensive margin*):

- ▶ Extensive margin (“EM”): # of products traded (weighted by share of imports from all partners)

$$EM_{ijt} = \frac{\sum_{k \in \Omega_{ij}} X_{Wjkt}}{\sum_{k \in \Omega_{Wj}} X_{Wjkt}}.$$

- ▶ Intensive margin (“IM”):  $i$ 's market share in  $j$ 's import market, for the goods that  $i$  exports to  $j$

$$IM_{ijt} = \frac{\sum_{k \in \Omega_{ij}} X_{ijkt}}{\sum_{k \in \Omega_{ij}} X_{Wjkt}}.$$

- ▶ Note that

$$\ln EM_{ijt} + \ln IM_{ijt} = \ln \sum_{k \in \Omega_{ij}} X_{ijkt} - \ln \sum_{k \in \Omega_{Wj}} X_{Wjkt} = \ln X_{ijt} / X_{Wjt},$$

which allows for an intuitive decomposition of aggregate trade.

## “Extensive Margin” vs. “Intensive Margin” (OLS)

|   | Dependent variables (based on Aggregate Manufacturing Trade) |                    |                     |                     |                      |                      |                     |                     |                     |
|---|--|--------------------|---------------------|---------------------|----------------------|----------------------|---------------------|---------------------|---------------------|
|   | ln Trade<br>(1)  | ln EM<br>(2)       | ln IM<br>(3)        | ln Trade<br>(4)     | ln EM<br>(5)         | ln IM<br>(6)         | ln Trade<br>(7)     | ln EM<br>(8)        | ln IM<br>(9)        |
| All FTAs  | 0.149***<br>(0.031)  | 0.056**<br>(0.023) | 0.087***<br>(0.027) | 0.071<br>(0.052)    | 0.243***<br>(0.044)  | -0.192***<br>(0.052) |                     |                     |                     |
| All FTAs, 4 yr lag                                  |  |                    |                     | 0.082<br>(0.051)    | -0.198***<br>(0.041) | 0.295***<br>(0.050)  |                     |                     |                     |
| Regular FTAs  |  |                    |                     |                     |                      |                      | 0.144***<br>(0.031) | 0.053**<br>(0.023)  | 0.085***<br>(0.027) |
| Deep FTAs   |  |                    |                     |                     |                      |                      | 0.314***<br>(0.053) | 0.180***<br>(0.044) | 0.153***<br>(0.050) |
| <i>Total FTA Effects (main effect + 4 year lag)</i> |  |                    |                     |                     |                      |                      |                     |                     |                     |
| All FTAs, total                                     |  |                    |                     | 0.153***<br>(0.032) | 0.046*<br>(0.023)    | 0.103***<br>(0.027)  |                     |                     |                     |
| Exporter-time FEs                                   | x  | x                  | x                   | x                   | x                    | x                    | x                   | x                   | x                   |
| Importer-time FEs                                   | x  | x                  | x                   | x                   | x                    | x                    | x                   | x                   | x                   |
| Pair FEs  | x  | x                  | x                   | x                   | x                    | x                    | x                   | x                   | x                   |
| Observations  | 56201  | 54169              | 53924               | 56201               | 54169                | 53924                | 56201               | 54169               | 53924               |

Aggregate bilateral trade flows between 116 countries over the period 1991-2015, using every 4 years. “Deep” FTA refers to customs unions and/or common markets. Standard errors, which appear in parentheses, are clustered by pair. \*  $p < 0.10$ , \*\*  $p < .05$ , \*\*\*  $p < .01$ .

- ▶ These results create the impression that most of the effect of FTAs on trade is through the *intensive* margin.

## Product-level Results (Reveals aggregation bias)

|   | Dependent variable: SITC3 *5 digit* Trade Flows 1991-2015 |     |     |     |     |     |     |
|---|---|-----|-----|-----|-----|-----|-----|
|   | (1)   | (2) | (3) | (4) | (5) | (6) | (7) |
| All FTAs  | 0.113***  |     |     |     |     |     |     |
|   | (0.034)   |     |     |     |     |     |     |
| All FTAs, 4 yr lag                                  |   |     |     |     |     |     |     |
| All FTAs, 4 yr lead                                 |   |     |     |     |     |     |     |
| Regular FTAs  |   |     |     |     |     |     |     |
| Deep FTAs   |   |     |     |     |     |     |     |
| <i>Total FTA Effects (main effect + 4 year lag)</i> |   |     |     |     |     |     |     |
| All FTAs, total                                     |   |     |     |     |     |     |     |
| Exporter-time FEs                                   | x   |     |     |     |     |     |     |
| Importer-time FEs                                   | x   |     |     |     |     |     |     |
| Pair FEs  | x   |     |     |     |     |     |     |
| Exporter-product-time FEs                           |   |     |     |     |     |     |     |
| Importer-product-time FEs                           |   |     |     |     |     |     |     |
| Product-pair FEs                                    |   |     |     |     |     |     |     |
| Observations  | 42,721,982  |     |     |     |     |     |     |

Pooled, unbalanced sample of 5 digit SITC3 bilateral trade flows for 2,771 product categories between 116 countries over the period 1991-2015, using every 4 years. Standard errors are clustered by pair . \*  $p < 0.10$  , \*\*  $p < .05$  , \*\*\*  $p < .01$ .

If we keep the FEs the same, pooling across disaggregated products leads to the *exact same estimates* we found for aggregate data. This is due to the special properties of PPML.

## Product-level Results (Reveals aggregation bias)

|   | Dependent variable: SITC3 *5 digit* Trade Flows 1991-2015 |            |            |            |     |     |     |
|---|---|------------|------------|------------|-----|-----|-----|
|   | (1)   | (2)        | (3)        | (4)        | (5) | (6) | (7) |
| All FTAs  | 0.113***  | 0.069***   | 0.114***   | 0.054***   |     |     |     |
|   | (0.034)   | (0.022)    | (0.034)    | (0.020)    |     |     |     |
| All FTAs, 4 yr lag                                  |   |            |            |            |     |     |     |
| All FTAs, 4 yr lead                                 |   |            |            |            |     |     |     |
| Regular FTAs  |   |            |            |            |     |     |     |
| Deep FTAs   |   |            |            |            |     |     |     |
| <i>Total FTA Effects (main effect + 4 year lag)</i> |   |            |            |            |     |     |     |
| All FTAs, total                                     |   |            |            |            |     |     |     |
| Exporter-time FEs                                   | x   |            | x          |            |     |     |     |
| Importer-time FEs                                   | x   |            | x          |            |     |     |     |
| Pair FEs  | x   | x          |            |            |     |     |     |
| Exporter-product-time FEs                           |   | x          |            | x          |     |     |     |
| Importer-product-time FEs                           |   | x          |            | x          |     |     |     |
| Product-pair FEs                                    |   |            | x          | x          |     |     |     |
| Observations  | 42,721,982  | 39,769,036 | 42,692,796 | 39,663,541 |     |     |     |

Pooled, unbalanced sample of 5 digit SITC3 bilateral trade flows for 2,771 product categories between 116 countries over the period 1991-2015, using every 4 years. Standard errors are clustered by pair . \*  $p < 0.10$  , \*\*  $p < .05$  , \*\*\*  $p < .01$ .

Interacting the different fixed effects with the product dimension then isolates different sources of aggregation bias.



## Product-level Results (Reveals aggregation bias)

| Dependent variable: SITC3 *5 digit* Trade Flows 1991-2015 |                     |                     |                     |                     |                     |                     |                     |
|---|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|   | (1)                 | (2)                 | (3)                 | (4)                 | (5)                 | (6)                 | (7)                 |
| All FTAs  | 0.113***<br>(0.034) | 0.069***<br>(0.022) | 0.114***<br>(0.034) | 0.054***<br>(0.020) |                     | 0.061***<br>(0.019) | 0.055***<br>(0.017) |
| All FTAs, 4 yr lag  |                     |                     |                     |                     |                     | -0.020<br>(0.015)   |                     |
| All FTAs, 4 yr lead                                       |                     |                     |                     |                     |                     |                     | -0.001<br>(0.020)   |
| Regular FTAs  |                     |                     |                     |                     | 0.052***<br>(0.020) |                     |                     |
| Deep FTAs   |                     |                     |                     |                     | 0.153***<br>(0.040) |                     |                     |
| <i>Total FTA Effects (main effect + 4 year lag)</i>       |                     |                     |                     |                     |                     |                     |                     |
| All FTAs, total   |                     |                     |                     |                     |                     | 0.040<br>(0.025)    |                     |
| Exporter-time FEs   | x                   |                     | x                   |                     |                     |                     |                     |
| Importer-time FEs   | x                   |                     | x                   |                     |                     |                     |                     |
| Pair FEs  | x                   | x                   |                     |                     |                     |                     |                     |
| Exporter-product-time FEs                                 |                     | x                   |                     | x                   | x                   | x                   | x                   |
| Importer-product-time FEs                                 |                     | x                   |                     | x                   | x                   | x                   | x                   |
| Product-pair FEs  |                     |                     | x                   | x                   | x                   | x                   | x                   |
| Observations  | 42,721,982          | 39,769,036          | 42,692,796          | 39,663,541          | 39,663,541          | 39,663,541          | 38,216,197          |

Pooled, unbalanced sample of 5 digit SITC3 bilateral trade flows for 2,771 product categories between 116 countries over the period 1991-2015, using every 4 years. Standard errors are clustered by pair. \*  $p < 0.10$ , \*\*  $p < .05$ , \*\*\*  $p < .01$ .

Other specifications yield different conclusions than what we saw w/ aggregate data. Column 5 shows Deep FTAs have much larger effects than other FTAs. Column 6 fails to find lagged effects of FTAs.

## More Disaggregated Results

| <b>Dependent variable: SITC3 Manufacturing Trade 1991-2015</b> |                     |                     |                     |                     |                     |                     |
|--|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|  | <i>Aggregate</i>    | <i>1 digit SITC</i> | <i>2 digit SITC</i> | <i>3 digit SITC</i> | <i>4 digit SITC</i> | <i>5 digit SITC</i> |
|  | (1)                 | (2)                 | (3)                 | (4)                 | (5)                 | (6)                 |
| All FTAs   | 0.113***<br>(0.034) | 0.075***<br>(0.025) | 0.058***<br>(0.021) | 0.057***<br>(0.020) | 0.057***<br>(0.019) | 0.054***<br>(0.020) |
| # products / industries  | 1                   | 10                  | 63                  | 231                 | 895                 | 2,771               |
| Observations   | 60,614              | 449,390             | 2,295,015           | 6,743,206           | 18,795,101          | 39,663,541          |

Pooled, unbalanced sample of SITC3 bilateral trade flows between 116 countries over the period 1991-2015, using every 4 years. All estimates include exporter-(SITC)-time, importer-(SITC)-time, and exporter-importer-(SITC) FEs. Standard errors are clustered by pair. \*  $p < 0.10$  , \*\*  $p < .05$  , \*\*\*  $p < .01$ .

## Sidebar: why are product-level results and aggregate results different?

Using the model from French (2016), the elasticity of aggregate trade with respect to trade barriers is

$$\varepsilon_{ij} = -\theta + \frac{\partial \left( \tilde{T}_{ij} / \tilde{T}_{jj} \right)}{\partial \ln d_{ij}}$$

where

- ▶  $\theta$ : typical trade elasticity parameter (think Frchet disp. parameter from an Eaton-Kortum model)
- ▶  $\tilde{T}_{ij} / \tilde{T}_{jj}$  captures “product-level comparative advantage” between  $i$  and  $j$

$$\tilde{T}_{ij} := \sum_k \left( \frac{P_{jk}}{P_j} \right)^{\theta - (\sigma - 1)} \frac{T_{ik}}{T_i}$$

- ◊  $T_{ik}$  is  $i$ 's technology level for good  $k$ ;  $T_i$  is  $i$ 's aggregate technology level
- ◊  $P_{jk}$  is the price of good  $k$  in  $j$ ;  $P_j$  is the aggregate price level in  $j$ .
- ◊  $\sigma < \theta + 1$  is the elasticity of substitution across products

## Sidebar: why are product-level results and aggregate results different?

Using the model from French (2016), the elasticity of aggregate trade with respect to trade barriers is

$$\varepsilon_{ij} = -\theta + \frac{\partial(\tilde{T}_{ij}/\tilde{T}_{jj})}{\partial \ln d_{ij}}$$

where

- ▶  $\theta$ : typical trade elasticity parameter (think Frchet disp. parameter from an Eaton-Kortum model)
- ▶  $\tilde{T}_{ij}/\tilde{T}_{jj}$  captures “product-level comparative advantage” between  $i$  and  $j$ .

If  $T_{ik}$ 's are fixed, one can show that  $\frac{\partial(\tilde{T}_{ij}/\tilde{T}_{jj})}{\partial \ln d_{ij}} > 0$ .

Thus, for aggregate estimates of  $\theta$  to be *upward*-biased, one would need  $T_{ik}$ 's for each country's (bilateral) comparative advantage products to increase after trade liberalization occurs

**Table: Effects of FTAs on “Least-traded” Products - Pooled PPML**

|   | Dependent variable: SITC3 5 digit Trade Flows 1991-2015 |                     |                     |                      |                      |                      |                      |                     |                     |
|---|---|---------------------|---------------------|----------------------|----------------------|----------------------|----------------------|---------------------|---------------------|
|   | (1)   | (2)                 | (3)                 | (4)                  | (5)                  | (6)                  | (7)                  | (8)                 | (9)                 |
| <i>Pooled FTA Effects across all products</i>                   |   |                     |                     |                      |                      |                      |                      |                     |                     |
| All FTAs  | 0.054***<br>(0.020)                                     | 0.061***<br>(0.019) |                     | -0.104***<br>(0.023) | -0.045**<br>(0.021)  |                      | -0.107***<br>(0.025) | -0.102**<br>(0.045) | -0.028<br>(0.025)   |
| All FTAs <sub>t-4</sub>   |   | -0.020<br>(0.015)   |                     |                      | -0.139***<br>(0.017) |                      |                      |                     |                     |
| Reg. FTAs   |   |                     | 0.052***<br>(0.020) |                      |                      | -0.075***<br>(0.022) |                      |                     |                     |
| Deep FTAs   |   |                     | 0.153***<br>(0.040) |                      |                      | 0.193***<br>(0.044)  |                      |                     |                     |
| <i>FTA Effects for LTPs</i>                                     |   |                     |                     |                      |                      |                      |                      |                     |                     |
| All FTAs × $\mathbf{1}_{k \notin \Omega_{ij}^*}$                |   |                     |                     | 0.741***<br>(0.038)  | 0.599***<br>(0.036)  |                      | 0.656***<br>(0.027)  | 1.163***<br>(0.068) | 0.379***<br>(0.025) |
| All FTAs <sub>t-4</sub> × $\mathbf{1}_{k \notin \Omega_{ij}^*}$ |   |                     |                     |                      | 0.284***<br>(0.023)  |                      |                      |                     |                     |
| Reg. FTAs × $\mathbf{1}_{k \notin \Omega_{ij}^*}$               |   |                     |                     |                      |                      | 0.541***<br>(0.029)  |                      |                     |                     |
| Deep FTAs × $\mathbf{1}_{k \notin \Omega_{ij}^*}$               |   |                     |                     |                      |                      | 1.190***<br>(0.037)  |                      |                     |                     |
| <i>Total FTA Effects (main effect + 4 year lag)</i>             |   |                     |                     |                      |                      |                      |                      |                     |                     |
| Total All FTAs  |   | 0.040               |                     |                      | -0.184***            |                      |                      |                     |                     |
| Total All FTAs × $\mathbf{1}_{k \notin \Omega_{ij}^*}$          |   |                     |                     |                      | 0.882***             |                      |                      |                     |                     |
| <i>ikt and jkt FEs</i>  | x   | x                   | x                   | x                    | x                    | x                    | x                    |                     | x                   |
| <i>it and jt FEs</i>  |   |                     |                     |                      |                      |                      |                      | x                   |                     |
| <i>ijk FEs</i>  | x   | x                   | x                   | x                    | x                    | x                    | x                    | x                   | x                   |
| Percentile definition   | -   | -                   | -                   | raw                  | raw                  | raw                  | relative             | raw                 | Kehoe-Ruhl          |
| Observations  | 39,663,541  | 39,663,541          | 39,663,541          | 39,663,541           | 39,663,541           | 39,663,541           | 39,663,541           | 42,692,796          | 42,692,796          |

Pooled sample of 5 digit SITC3 trade flows between 116 countries over the period 1991-2015, every 4 years.  $\mathbf{1}_{k \notin \Omega_{ij}^*}$  is indicator equal to 1 if trade in product  $k$  was not intensively traded in years preceding FTA. Columns 5, 6, 7, and 9 compute this measure using raw percentiles, whereas column 9 uses relative percentiles, relative to each product's contribution to world trade. Column 9 uses the average of 2-4 years before the FTA. Standard errors are clustered by pair. \*  $p < 0.10$ , \*\*  $p < .05$ , \*\*\*  $p < .01$ .

Table: "Least-traded" Products - more results

|   | Dependent variable: SITC3 5 digit Trade Flows 1991-2015 |                     |                      |                      |                      |                      |                      |                      |
|---|---|---------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
|   | (1)   | (2)                 | (3)                  | (4)                  | (5)                  | (6)                  | (7)                  | (8)                  |
| <i>Control for if trade in LTPs generally grows faster than trade in other products for all pairs</i> |   |                     |                      |                      |                      |                      |                      |                      |
| $[X_{ijk1} < 10\text{th perc.}] \times (\text{year} - \text{first year})$                             |   | 0.046***<br>(0.001) |                      | 0.044***<br>(0.001)  |                      | 0.044***<br>(0.001)  | 0.044***<br>(0.001)  |                      |
| <i>Pooled FTA Effects across all products</i>   |   |                     |                      |                      |                      |                      |                      |                      |
| All FTAs  | 0.054***<br>(0.020)                                     | 0.060***<br>(0.018) | -0.104***<br>(0.023) | -0.074***<br>(0.021) | -0.112***<br>(0.021) | -0.081***<br>(0.019) | -0.036*<br>(0.020)   | -0.250***<br>(0.046) |
| $\times [\bar{X}_{ijk} < 10\text{th perc.}]$  |   |                     | 0.741***<br>(0.038)  | 0.628***<br>(0.038)  | 0.788***<br>(0.038)  | 0.697***<br>(0.035)  | 0.489***<br>(0.036)  | 0.864***<br>(0.058)  |
| $\times [10\text{th perc.} \leq \bar{X}_{ijk} < 40\text{th perc.}]$                                   |   |                     |                      |                      |                      |                      |                      | 0.231***<br>(0.047)  |
| $\times [40\text{th perc.} \leq \bar{X}_{ijk} < 70\text{th perc.}]$                                   |   |                     |                      |                      |                      |                      |                      | 0.099**<br>(0.041)   |
| All FTAs <sub>t+4</sub>   |   |                     |                      |                      | 0.018<br>(0.021)     | 0.014<br>(0.021)     |                      |                      |
| $\times [\bar{X}_{ijk} < 10\text{th perc.}]$  |   |                     |                      |                      | -0.089***<br>(0.030) | -0.129***<br>(0.032) |                      |                      |
| All FTAs <sub>t-4</sub>   |   |                     |                      |                      |                      |                      | -0.069***<br>(0.015) |                      |
| $\times [\bar{X}_{ijk} < 10\text{th perc.}]$  |   |                     |                      |                      |                      |                      | 0.192***<br>(0.022)  |                      |
| <i>Total FTA Effects (main effect + 4 year lag)</i>   |   |                     |                      |                      |                      |                      |                      |                      |
| Total All FTAs  |   |                     |                      |                      |                      |                      | -0.105***            |                      |
| $\times [\bar{X}_{ijk} < 10\text{th perc.}]$  |   |                     |                      |                      |                      |                      | 0.681***             |                      |
| <i>ikt, jkt and jik FEs</i>   | x   | x                   | x                    | x                    | x                    | x                    | x                    | x                    |
| Observations  | 39,663,541  | 39,663,541          | 39,663,541           | 39,663,541           | 38,216,197           | 38,216,197           | 39,663,541           | 39,663,541           |

Pooled sample of 5 digit SITC3 trade flows between 116 countries over the period 1991-2015, every 4 years.  $\bar{X}_{ijk}$  is the average trade flow for product  $k$  for years before  $i$  and  $j$  sign an FTA.  $X_{ij1}$  is the trade flow from the first year pair  $ij$  appears in the data. Standard errors are clustered by pair. \*  $p < 0.10$ , \*\*  $p < .05$ , \*\*\*  $p < .01$ .

Interestingly, trade in LTPs is generally growing relative to trade in other products over time. FTAs are shown to accelerate this process.

## Results from higher levels of aggregation

Table: "Least-traded" Products - more results

|   | Dependent variable: SITC3 5 digit Trade Flows 1991-2015 |                      |                     |                      |                      |                      |
|---|---|----------------------|---------------------|----------------------|----------------------|----------------------|
|   | 2 digit SITC  |                      | 3 digit SITC        |                      | 4 digit SITC         |                      |
| <i>Pooled FTA Effects across all products</i>         |   |                      |                     |                      |                      |                      |
| All FTAs  | -0.006<br>(0.022)                                       | -0.111***<br>(0.019) | -0.030<br>(0.022)   | -0.117***<br>(0.019) | -0.066***<br>(0.022) | -0.199***<br>(0.033) |
| × [ $\bar{X}_{ijk} < 10\text{th perc.}$ ]             | 0.383***<br>(0.038)                                     | 0.497***<br>(0.050)  | 0.497***<br>(0.038) | 0.593***<br>(0.051)  | 0.629***<br>(0.038)  | 0.771***<br>(0.050)  |
| × [10th perc. ≤ $\bar{X}_{ijk} < 40\text{th perc.}$ ] |   | 0.181***<br>(0.032)  |                     | 0.169***<br>(0.033)  |                      | 0.213***<br>(0.029)  |
| × [40th perc. ≤ $\bar{X}_{ijk} < 70\text{th perc.}$ ] |   | 0.053*<br>(0.032)    |                     | 0.023<br>(0.029)     |                      | 0.077***<br>(0.024)  |
| <i>ikt, jkt and ijk FEs</i>                           | x   | x                    | x                   | x                    | x                    | x                    |
| Observations  | 2,295,015   | 2,295,015            | 6,743,206           | 6,743,206            | 18,795,101           | 18,795,101           |

Pooled sample of SITC3 trade flows between 116 countries over the period 1991-2015 at different levels of disaggregation, every 4 years.

$\bar{X}_{ijk}$  is the average trade flow for product  $k$  for years before  $i$  and  $j$  sign an FTA. Standard errors are clustered by pair.

\*  $p < 0.10$ , \*\*  $p < .05$ , \*\*\*  $p < .01$ .

Even for relatively aggregated (2 digit) data, trade actually *decreases* for the goods that lie above the 40% percentile.

## Some thoughts on theoretical explanations

What model features could explain these patterns? Some ideas:

- ▶ *Within-origin substitutability*: purchasers in the destination balance purchases of products from each origin against other products from the same origin.
  - ◊ Crowley, Han, and Prayer (2022)
- ▶ *Link-specific capital*: scarcity of trade-specific capital leads to higher trade costs for large exporters when new exporters enter.
  - ◊ Bergin and Lin (2012); Feng, Li, and Swenson (2016); Bergin, Feng, and Lin (2018)



## Summary

**In brief:** We use product-level gravity to test some influential observations by Kehoe and Ruhl (2013) regarding trade growth in “less-traded products” following liberalization.

### Some takeaways:

- ◇ We confirm trade in less-traded and newly traded products grows much faster than trade in other products following trade liberalization, after taking into account technological change, multilateral resistance, and aggregation bias
- ◇ **Puzzle:** do not find other deciles contribute to aggregate trade growth; LTPs completely explain all aggregate trade growth
- ◇ We find increases in bilateral trade are generally biased towards less-traded products, even independently of FTAs
- ◇ Product-level results generally indicate upward bias in aggregate estimates

## Next steps...

Different paths to pursue from here:

- ▶ What drives stark difference between effects of FTAs on less-traded products versus more traded products?
  - ◊ Scarcity of trade-specific capital?
  - ◊ Substitutability between products from the same origin?
  - ◊ Within-pair product cycles?
- ▶ Role of product-level tariffs / elasticities.
- ▶ Crisper characterization of changing comparative advantages following FTAs + implications for welfare
- ▶ Bias corrections for PPML estimates

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## Other cases which aggregate consistently

**Eaton-Kortum model.** suppose:

- i.  $\sigma_k = \infty, \forall k$  (no national product differentiation)
- ii.  $T_{ik}$ 's  $\sim$  Frechet( $T_i^*, \theta$ ) (EK technology dispersion assumption)
- iii.  $d_{ijk} = d_{ij}$  (same bilateral trade friction for all products)

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- ii.  $T_{ik}$ 's  $\sim$  Frechet( $T_i^*, \theta$ ) (EK technology dispersion assumption)
- iii.  $d_{ijk} = d_{ij}$  (same bilateral trade friction for all products)

Then the aggregate-level trade share is given by

$$\pi_{ij} = \Gamma \frac{T_i^* (w_i d_{ij})^{-\theta}}{P_j^{*-\theta}}$$

where:

$$\Gamma \equiv \Gamma(\theta, \rho) \quad P_j^{*-\theta} = \Gamma^{-1} \sum_i T_i^* (w_i d_{ij}^*)^{-\theta}$$

The Frechet parameters  $T_i^*$  and  $\theta$  now provide technology levels and the trade elasticity.

## Other cases which aggregate consistently

**No Comparative Advantage.** suppose:

- i.  $\sigma_k = \sigma, \forall k$  (common trade elasticity across products)
- ii.  $T_{ik} = T_i^*, \forall k$  (no comparative advantage across products)
- iii.  $d_{ijk} \neq d_{ij}$  (trade frictions need not be uniform across products)

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- i.  $\sigma_k = \sigma, \forall k$  (common trade elasticity across products)
- ii.  $T_{ik} = T_i^*, \forall k$  (no comparative advantage across products)
- iii.  $d_{ijk} \neq d_{ij}$  (trade frictions need not be uniform across products)

Then the *aggregate*-level trade share is given by

$$\pi_{ij} = \frac{T_i^* (w_i d_{ij}^*)^{1-\sigma}}{P_j^{*1-\sigma}}$$

where:

$$\tau_{ij}^{*1-\sigma} = \sum_k d_{ijk}^{1-\sigma} \quad P_j^{*1-\sigma} = \sum_i T_i^* (w_i d_{ij}^*)^{1-\sigma}$$



## Gravity and the Different “Margins” of Trade

Following Hummels and Klenow (2005), the extensive margin (“EM”) may then be computed as

$$EM_{ijt} = \frac{\sum_{k \in \Omega_{ij}} X_{Wjkt}}{\sum_{k \in \Omega_{Wj}} X_{Wjkt}}. \quad (4)$$

where

- ▶ The “traded goods” set  $\Omega_{ij}$  is the set of products that lie above the 10th percentile when products are sorted by trade volume (as in Kehoe and Ruhl, 2013)
- ▶ Goods that fall below the 10th percentile are considered “least-traded”
- ▶ For ex ante measures, we combine trade data for each product from all years before the agreement
  - ◇ we also use combined trade data from 3 to 5 years before the agreement and find similar results
  - ◇ we also find similar results regardless if we use raw trade amounts vs. relative amounts (relative to total world trade in that product)

## Data - how and why we took care

From Kehoe and Ruhl (2013)'s appendix:

*"Unfortunately, the adoption of the Harmonized System—which took place in many countries in 1988 and in the United States in 1989—was accompanied by a significant change in the codes that are reported as traded."*

*"These problems seem less severe at more aggregate classifications; analysis at the two-digit level... may not be severely affected."*

*"It is worth noting that for both trade flows, the importing country seems to be less affected by the change in classification."*

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*"These problems seem less severe at more aggregate classifications; analysis at the two-digit level... may not be severely affected."*

*"It is worth noting that for both trade flows, the importing country seems to be less affected by the change in classification."*

What we did in response:

- ▶ We only used trade reported by the importing country
- ▶ We only included a country as an importer after they adopted SITC Rev. 3
  - ◊ SITC rev 3 adoption coincides with or follows HS adoption
- ▶ We did robustness for 4 digit-, 3 digit- and 2 digit-level aggregation levels

## Data - countries included by year

| year                      | number of countries |
|---------------------------|---------------------|
| 1991                      | 58                  |
| 1995                      | 87                  |
| 1999                      | 95                  |
| 2003                      | 106                 |
| 2007                      | 107                 |
| 2010                      | 103                 |
| 2015                      | 99                  |
| Total number of countries | 116                 |

## Model: General Framework

Utility is derived from CES preferences across a (discrete) large number of products:

$$U_i = \left[ \sum_{k=1}^K (q_i^k)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

where each  $q_i^k$  is a CES (Armington) aggregate across nationally differentiated varieties:

$$q_i^k = \left[ \sum_i^N (q_i^k)^{\frac{\xi^{k-1}}{\xi^k}} \right]^{\frac{\xi^k}{\xi^{k-1}}}$$

**Note:**  $\xi^k$  may vary by product,  $\sigma$  is global

## Model: Product-level Trade Shares

A generalized product-level gravity equation for country  $j$ 's trade share wrt origin  $i$ , product  $k$ :

$$\pi_{ijk} = \frac{T_{ik} (w_i d_{ijk})^{1-\xi^k}}{P_{jk}^{1-\xi^k}}$$

with:

- ◇  $T_{ik}$ : technology level
- ◇  $w_i$ : production cost
- ◇  $d_{ijk}$ : iceberg trade cost
- ◇  $P_{jk}^{1-\xi^k} \equiv \sum_i T_{ik} (c_{ik} d_{ijk})^{1-\xi^k}$  denotes the usual CES price index

(a.k.a. "inward multilateral resistance")

## Model: Conditions needed for *Aggregation*

**Special case.** suppose:

- i.  $\xi^k = \xi$  (common trade elasticity across products)
- ii.  $\xi = \sigma$  (same substitutability across vs. within product categories)
- iii.  $d_{ijk} = d_{ij}$  (same bilateral trade friction for all products)

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- iii.  $d_{ijk} = d_{ij}$  (same bilateral trade friction for all products)

Then the *aggregate*-level trade share is given by

$$\pi_{ij} = \frac{T_i^* (w_i d_{ij})^{1-\sigma}}{P_j^{*1-\sigma}}$$

where:

$$T_i^* = \sum_k T_{ik}; \quad P_j^{*1-\sigma} = \sum_i T_i^* (w_i d_{ij})^{1-\sigma}$$

→ In this special case, product-level gravity aggregates consistently to aggregate gravity.



## Model: Conditions needed for *Aggregation*

**More general cases.** suppose:

- i.  $\xi^k = \xi$  (common trade elasticity across products)
- ii.  $\sigma < \xi$  (varieties are more substitutable within product categories than across categories)
- iii.  $d_{ijk} = d_{ij}$  (same bilateral trade friction for all products)

## Model: Conditions needed for *Aggregation*

**More general cases.** suppose:

- i.  $\xi^k = \xi$  (common trade elasticity across products)
- ii.  $\sigma < \xi$  (varieties are more substitutable within product categories than across categories)
- iii.  $d_{ijk} = d_{ij}$  (same bilateral trade friction for all products)

Then the *aggregate*-level trade share is given by

$$\pi_{ij} = \frac{T_i^* (w_i d_{ij})^{1-\xi}}{P_j^{*1-\xi}} \times Z_{ij}$$

where:

$$Z_{ij} = \left\{ \sum_k \left( \frac{T_{ik}}{T_i^*} \right) \left( \frac{P_{jk}}{P_j^*} \right)^{\xi-\sigma} \right\}$$

is a non-trivial bilateral term reflecting product-level comparative advantage, such that estimates of  $\tau_{ij}$  will suffer from **aggregation bias**. (French, 2016)

## Model: Conditions needed for *Aggregation*

**More general cases.** suppose:

- i.  $\xi^k = \xi$  (common trade elasticity across products)
- ii.  $\sigma = \xi$  (same substitutability across vs. within product categories)
- iii.  $d_{ijk} \neq d_{ij}$  (non-uniform trade friction for all products)

## Model: Conditions needed for *Aggregation*

**More general cases.** suppose:

- i.  $\xi^k = \xi$  (common trade elasticity across products)
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- iii.  $d_{ijk} \neq d_{ij}$  (non-uniform trade friction for all products)

Then the *aggregate*-level trade share is given by

$$\pi_{ij} = \frac{T_i^* (w_i d_{ij}^*)^{1-\sigma}}{P_j^{*1-\sigma}}$$

where:

$$T_i^* = \sum_k T_{ik}; \quad d_{ij}^{*1-\sigma} = \sum_k \frac{T_{ik}}{T_i^*} d_{ijk}^{1-\sigma} \quad P_j^{*1-\sigma} = \sum_i T_i^* (w_i d_{ij}^*)^{1-\sigma}$$

→ Again, the bilateral term is inseparable from product-level comparative advantage.

## FTA Depth

Using BBF's classifications of agreement "depth" we can include 4 different PTA/FTA types:

- ▶ **One-way PTAs:** e.g., GSP and other non-reciprocal preference arrangements
- ▶ **Two-way PTAs:** Reciprocal trade agreements that stop short of completely eliminating barriers to trade
- ▶ **Free Trade Agreements:** Agreements explicitly committed to free trade
- ▶ **Economic Integration Agreements:** "Deeper" agreements with commitments that go beyond free trade
  - ◇ e.g., Customs Unions, Common Markets

**Note:** We generally find the first two categories do not have significant effects on trade on average; we thus mainly focus on the two "deepest" categories. [▶ back](#)